

CANDIDATE  
NAME

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**MATHEMATICS**

**9709/32**

Paper 3 Pure Mathematics 3 (P3)

**May/June 2017**

**1 hour 45 minutes**

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF9)

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

**DO NOT WRITE IN ANY BARCODES.**

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 75.

This document consists of **19** printed pages and **1** blank page.



















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(ii) Find the exact value approached by the mass of  $B$  as  $t$  becomes large. State what happens to the mass of  $A$  as  $t$  becomes large. [2]

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- (ii) On a sketch of an Argand diagram, shade the region whose points represent complex numbers  $z$  satisfying both the inequalities  $|z - u| < 1$  and  $|z| < |z + i|$ . [4]

- 7 (i) Prove that if  $y = \frac{1}{\cos \theta}$  then  $\frac{dy}{d\theta} = \sec \theta \tan \theta$ . [2]

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- (ii) Prove the identity  $\frac{1 + \sin \theta}{1 - \sin \theta} \equiv 2 \sec^2 \theta + 2 \sec \theta \tan \theta - 1$ . [3]

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(iii) Hence find the exact value of  $\int_0^{\frac{1}{4}\pi} \frac{1 + \sin \theta}{1 - \sin \theta} d\theta$ . [4]

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(ii) Find the equation of the plane through the origin which contains  $l$ . Give your answer in the form  $ax + by + cz = d$ . [3]

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(iii) Find the exact value of the perpendicular distance of  $A$  from this plane. [3]

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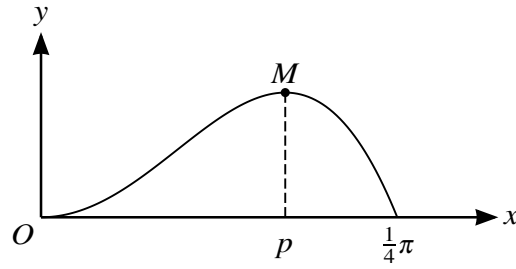
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The diagram shows the curve  $y = x^2 \cos 2x$  for  $0 \leq x \leq \frac{1}{4}\pi$ . The curve has a maximum point at  $M$  where  $x = p$ .

(i) Show that  $p$  satisfies the equation  $p = \frac{1}{2} \tan^{-1} \left( \frac{1}{p} \right)$ . [3]

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(ii) Use the iterative formula  $p_{n+1} = \frac{1}{2} \tan^{-1} \left( \frac{1}{p_n} \right)$  to determine the value of  $p$  correct to 2 decimal places. Give the result of each iteration to 4 decimal places. [3]

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